Lecture 2

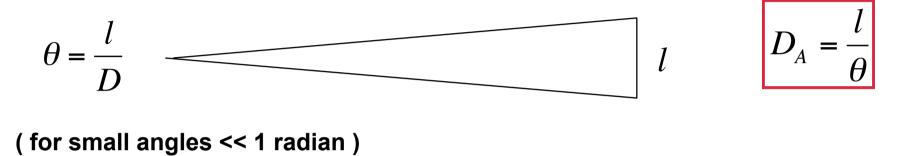
Astronomical Distances

Astronomical Distances

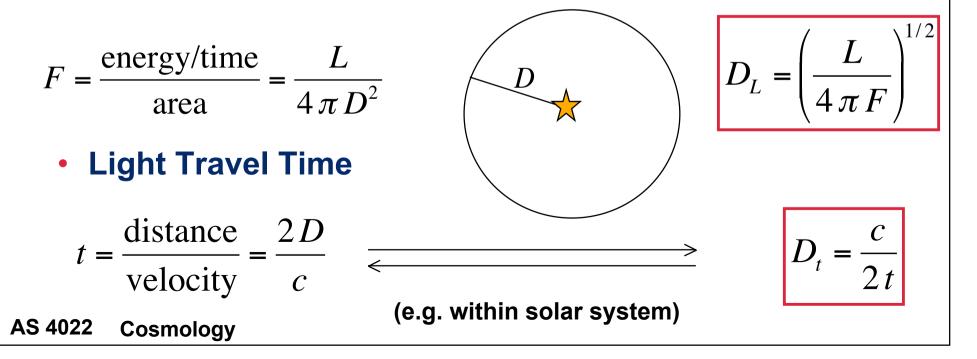
- Size of Earth
- Distance to the Moon (1 sec)
- Distance to the Sun (8 min)
- Distance to other stars (years)
- Distance to centre of our Galaxy (30,000 yr to centre)
- Distances to other Galaxies (2 million years to Andromeda)
- Size of the Universe (13 billion years)

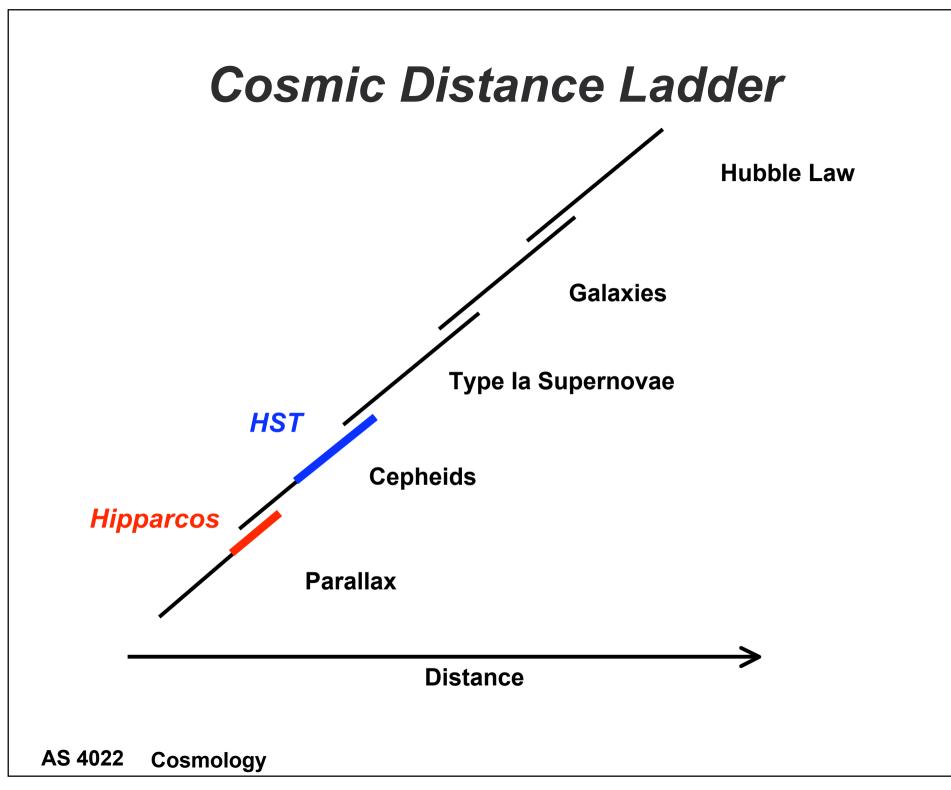
Distance Methods

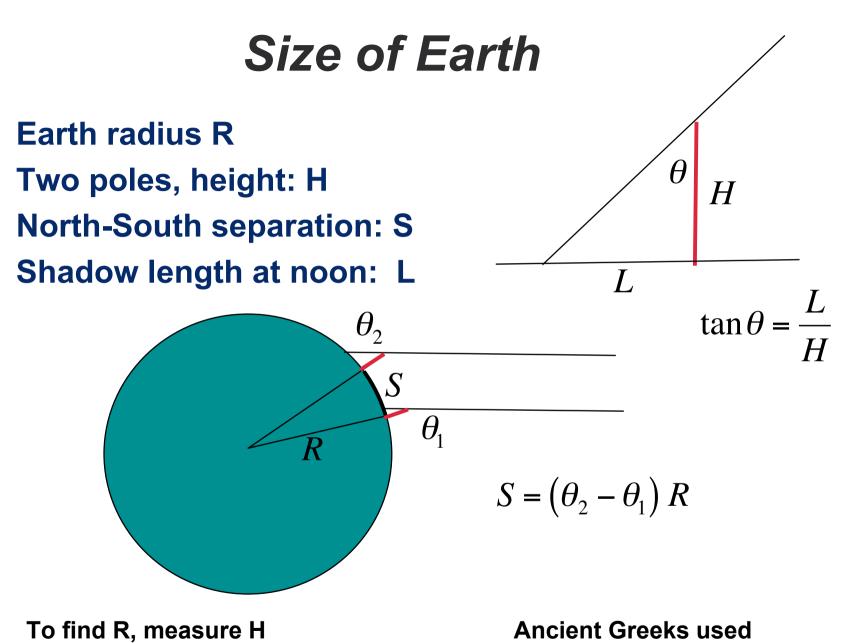
• Standard Rulers ==> Angular Size Distances



• Standard Candles ==> Luminosity Distances



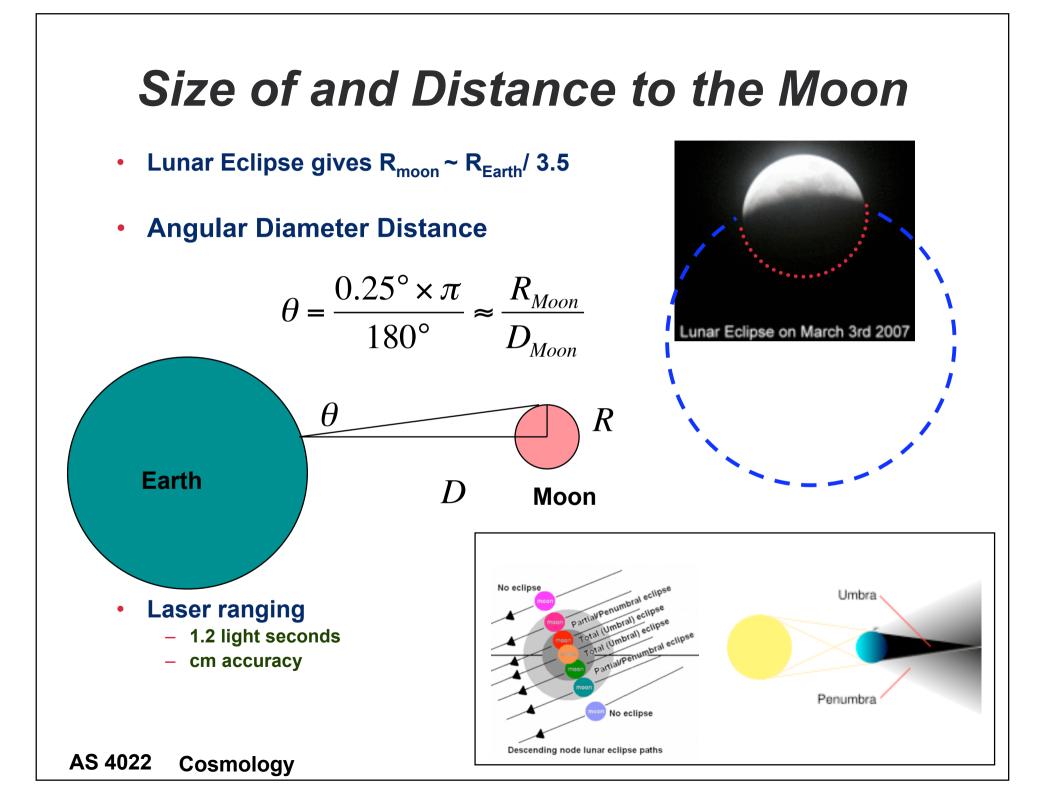


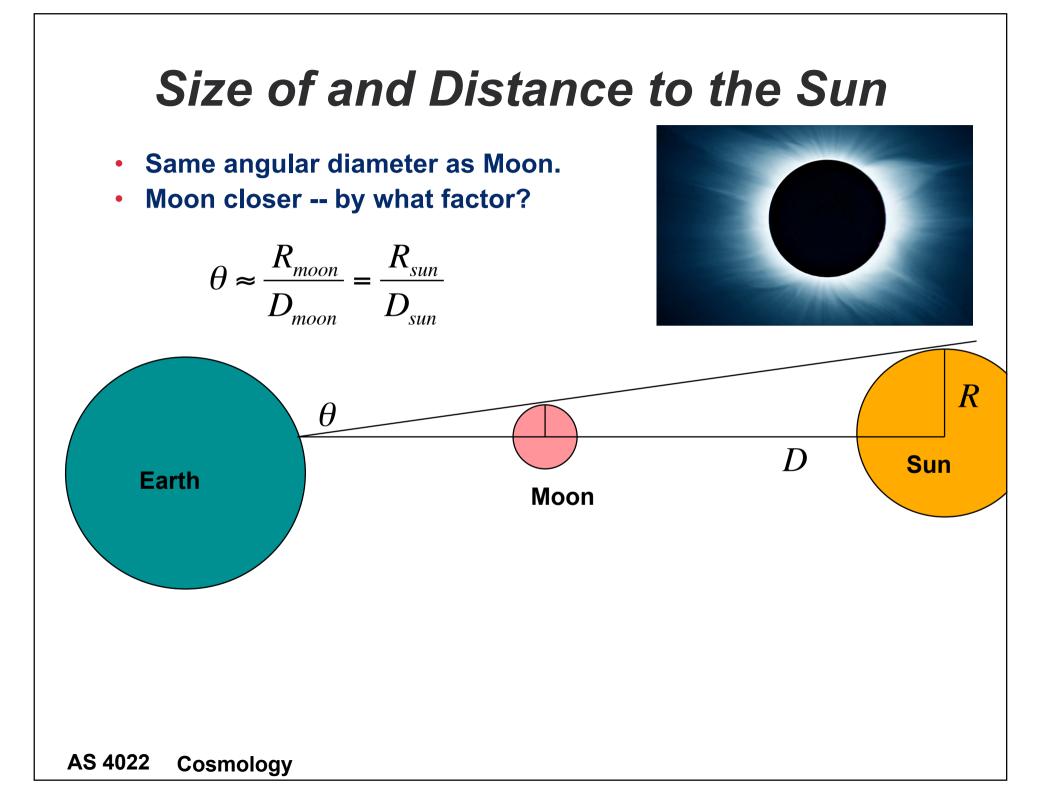


and L at 2 latitudes separated by S.

Ancient Greeks used Athens to Alexandria, finding R ~ 6300 km

AS 4022 Cosmology



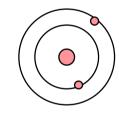


Earth's Orbit size from Jupiter's Moons

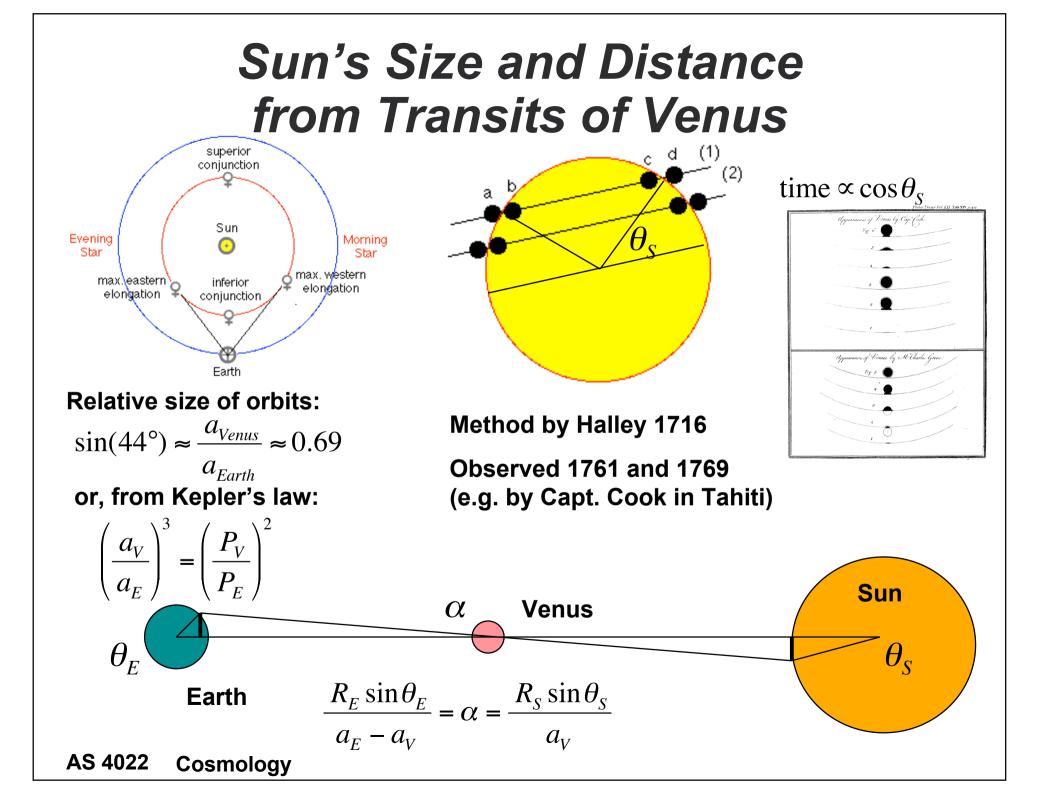
a_E = 1 AU = 8 light minutes

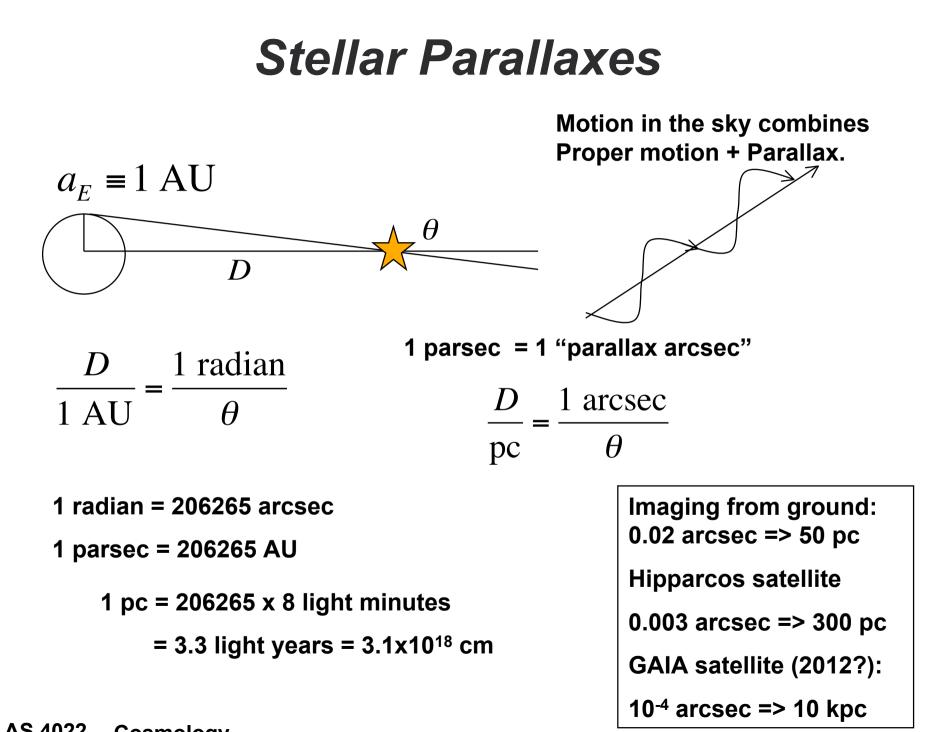
= 1.5 x 10¹³ cm





Due to light travel time across Earth's orbit, Jupiter's moons appear to orbit up to 8 minutes ahead or behind schedule.



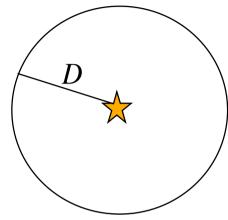


Luminosity Distances

Use the inverse-square law:

<i>F</i> =	L	_ energy/time
	$\overline{4\pi D^2}$	=area





Luminosity Distance:

Apparent magnitude: $m \equiv -2.5 \log(F/F_{Vega})$

e.g. 5 mags = 100x fainter = 10x farther away

0.1 mag = 10% fainter = 5% farther away

Absolute magnitude M

= apparent magnitude m at standard distance 10 pc

$$m = M + 5\log(D/10 \text{ pc})$$

 $(1.05)^2 \approx 1.1$

 $(1+x)^2 \approx 1+2x$

since $F \propto D^{-2}$

Distance Modulus (ignoring dust extinction):

$$m - M = 5\log(D/\mathrm{pc}) - 5$$

How Far are the Stars ?

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Sun : m_v = -24 mag
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Brightest stars (about 10) :
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 $m_v < +1 mag$

Faintest (naked-eye) stars (about 6000) :

 $m_v < + 6 mag$

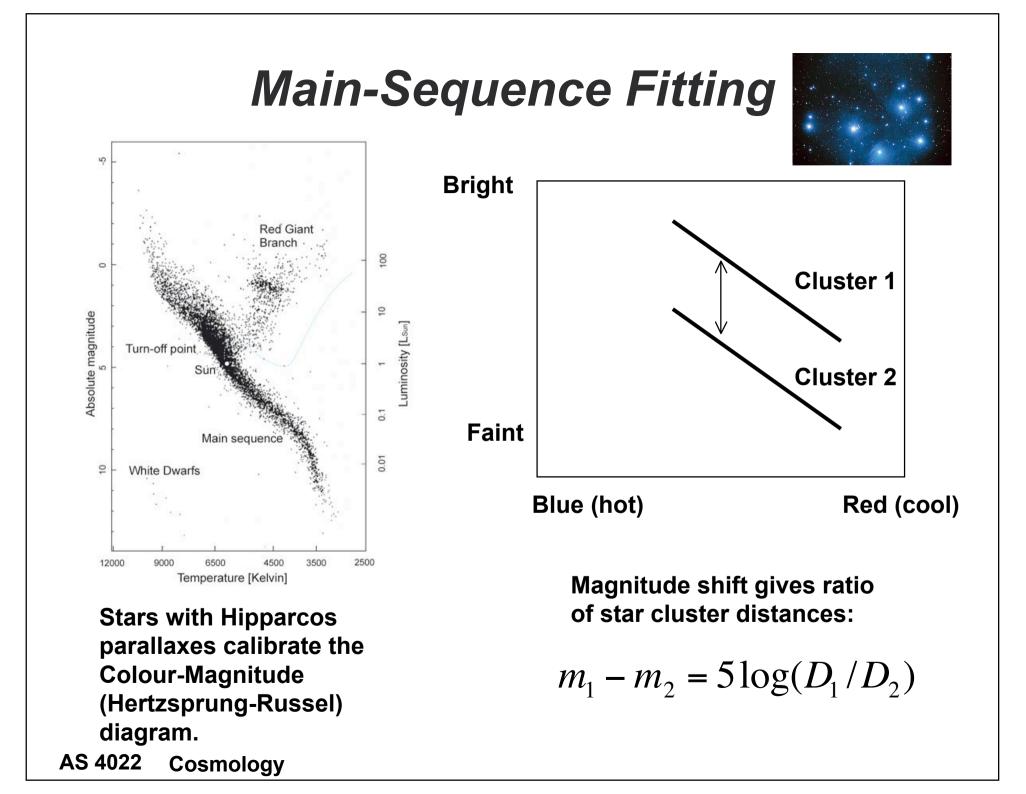
Relative distances :

5 mag = 100 x fainter = 10 x farther away

25 mag = 10^{10} x fainter = 10^5 x farther away

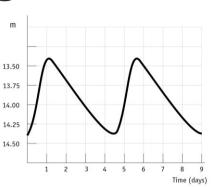
Distance to a sun-like $m_v = +1$ mag star:

8 x 10⁵ light minutes = 1.5 light years

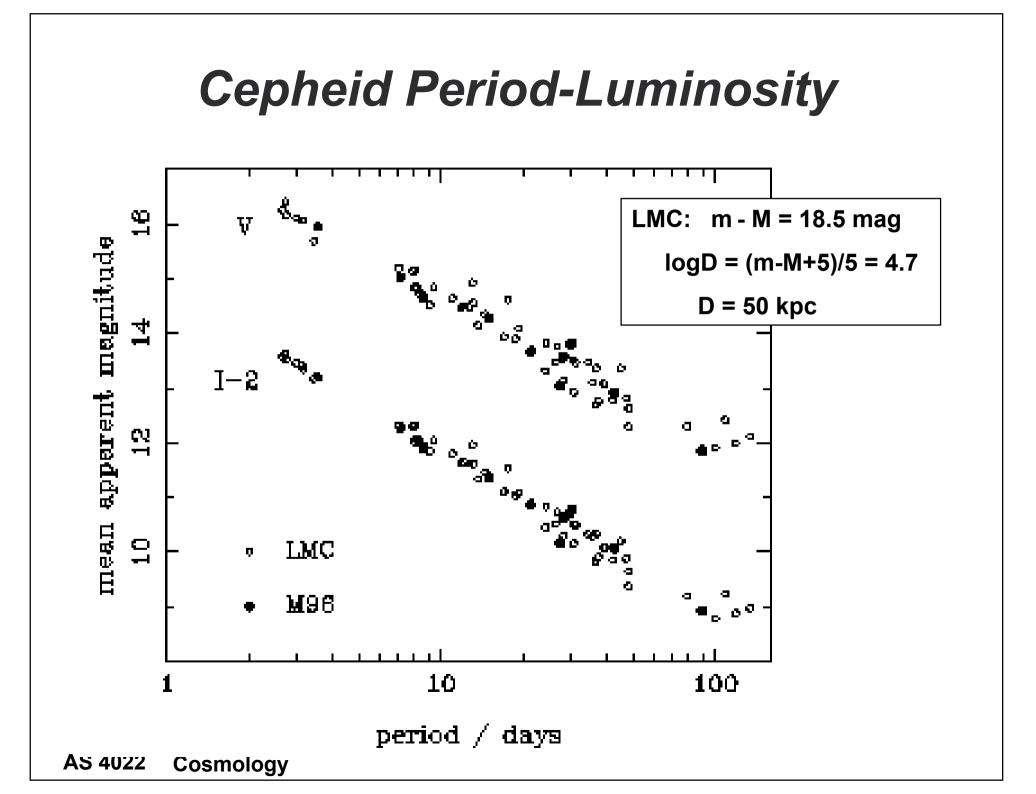


Cepheid Variable Stars

- H ionisation instability drives pulsations.
- Pulsation period ~ sound travel time
- Period-Luminosity relationship L ~ P^{1.3}



- Calibrate using parallax, main-sequence fitting.
- Also from Supernova 1987A, light travel time to circumstellar ring --> D_{LMC} = 51 kpc +/- 6%.
- Hubble used Cepheids in Local Group D < 2 Mpc.
- HST sees Cepheids in Virgo Cluster D < 20 Mpc.



Distance to the Galactic Centre

D(Galactic Centre) = 8.5 kpc

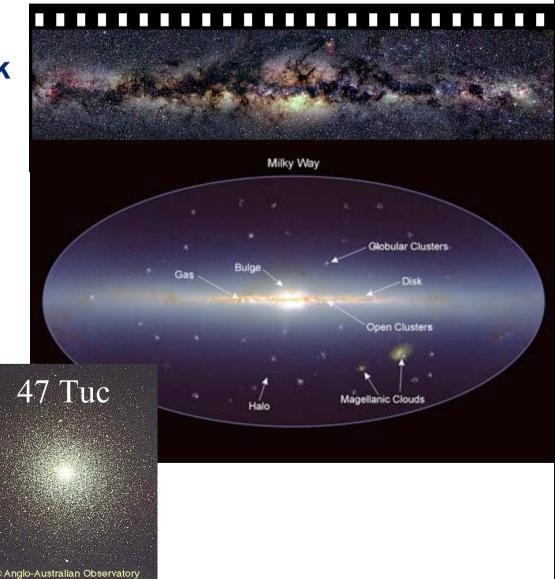
- Dust in Galactic Disk $A_V \approx 1 \mod / \text{kpc}$
- RR Lyr variables in Galactic Bulge

 $M_V(RR Lyr) \sim +0.5 mag$

Globular Clusters
in Galactic Halo

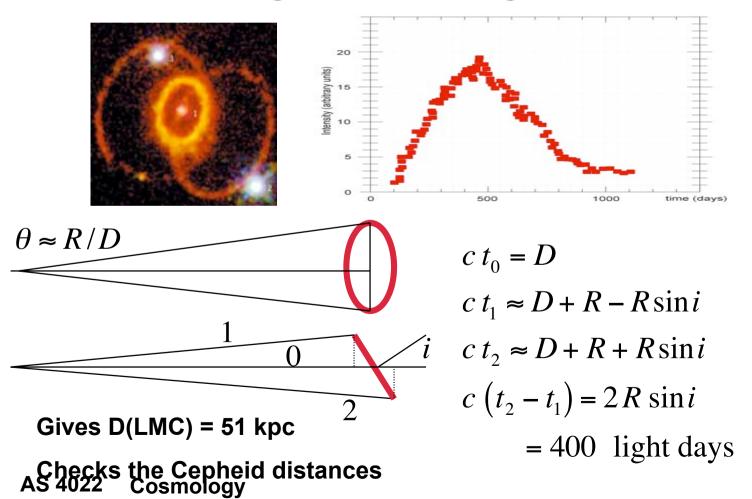
Cepheids

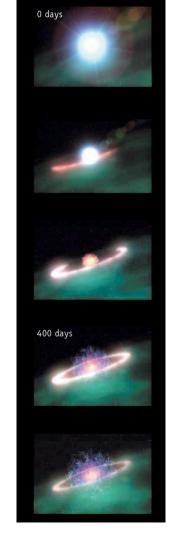
Main Sequence



Distance to Large Magellenic Cloud

- SN 1987a explosion illuminates circumstellar gas ring.
- Light travel time gives linear size.
- Observed angular size then gives distance.





Distances to Galaxies

Standard Candles ?

Cepheids (to 20 Mpc)

Brightest stars

Planetary nebulae

Globular Clusters

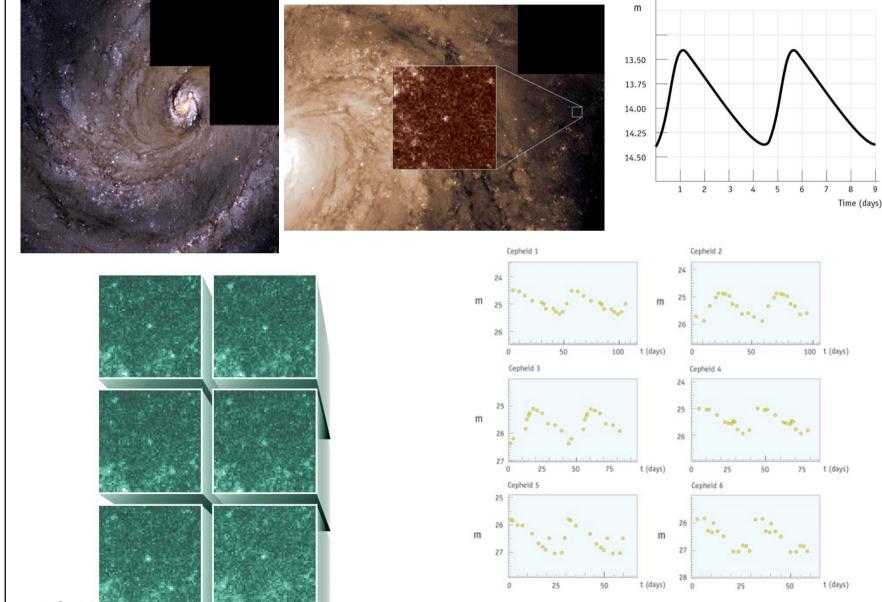
Supernovae (e.g. Type 1a 20-400 Mpc)

Galaxies (e.g. using Luminosity-Rotation Velocity correlations)

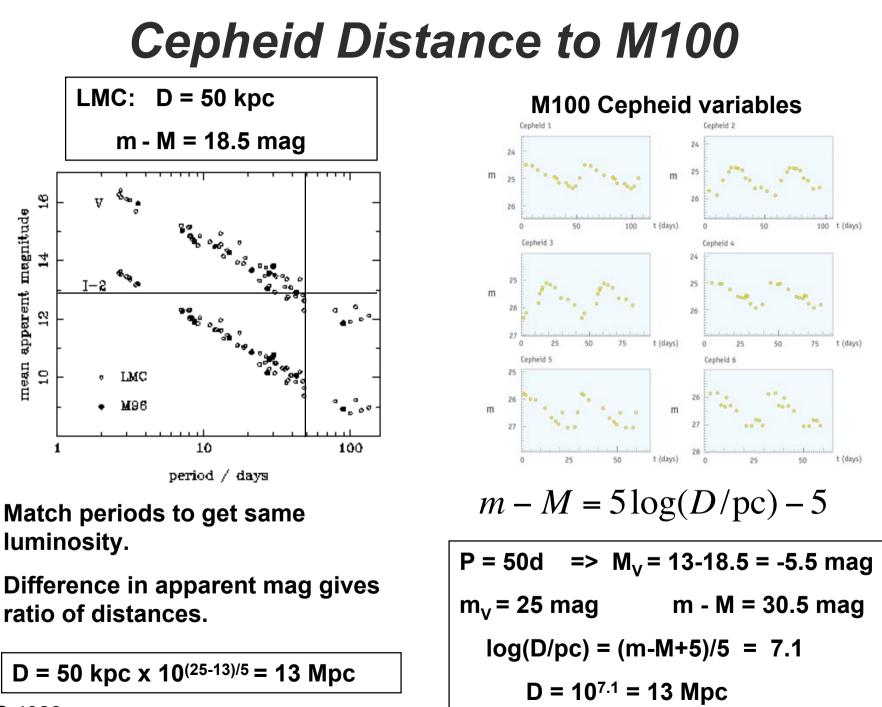


Giant Elliptical in Virgo Cluster $\sim 10^4$ globular clusters

HST designed to find Cepheids in Virgo Cluster Galaxies

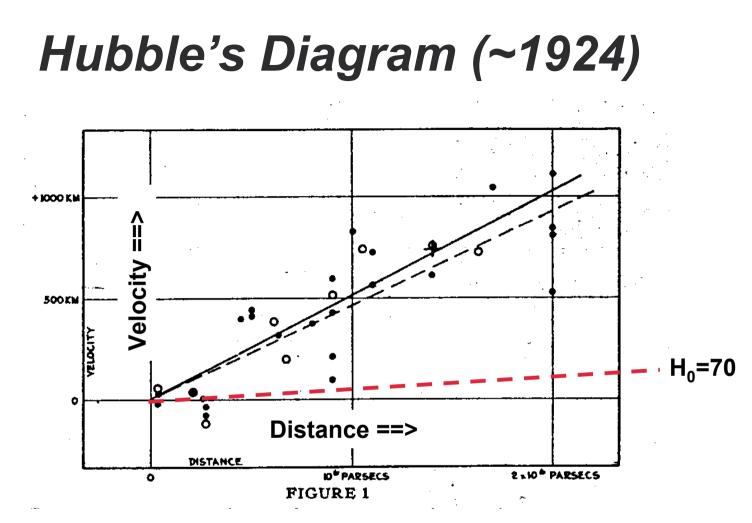


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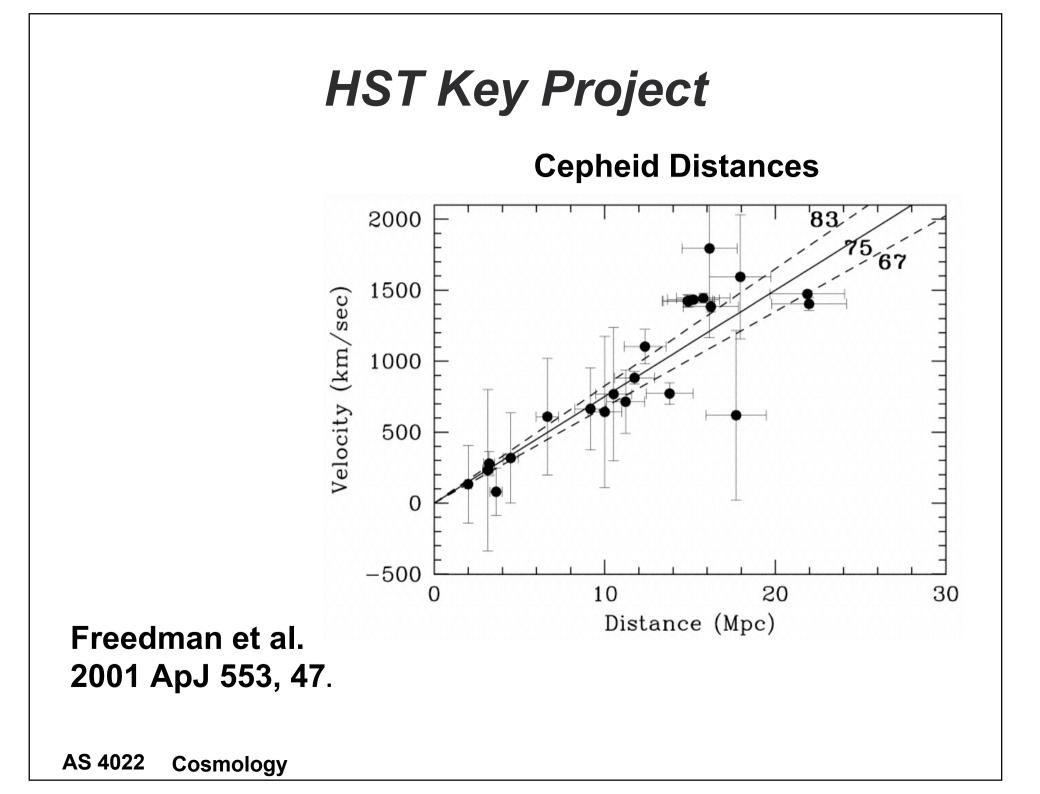
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mean apperent megnitude



Slope = H_0 = 500 km/s/Mpc (!) Cepheid distance calibration was wrong (dust in Milky Way was not yet recognised).

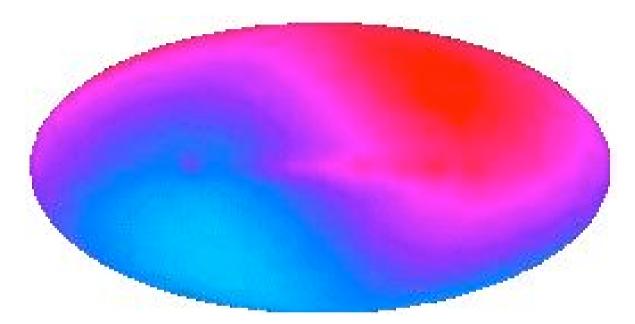
Hubble was wrong (but his idea was good).



Why go beyond Cepheids?

- HST sees Cepheids to D = 10-20 Mpc.
- $H_0 \ge D = 70 \ge 15 \sim 1000 \text{ km/s}$.
- not really far enough
- galaxy pecular velocities ~500 km/s.
- galaxies falling toward Virgo cluster.

CMB dipole --> Milky Way velocity



$$\frac{\Delta T}{T} \approx \frac{V}{c} \rightarrow V \approx 600 \text{ km s}^{-1}$$

Largely due to Milky Way (Local Group) falling toward Virgo Cluster.

SN Type Ia in Virgo Galaxy NGC 4526

Supernova outshines the entire galaxy, but only for a month or so.

Type II -- massive stars (M > 8 M_{SUN}) explode at end of life.

Type Ia -- white dwarf in a binary system accretes mass, collapses when $M_{WD} = 1.4 M_{SUN}$.

Good "standard bombs".



Calibrate SN distances using HST to see Cepheids in Virgo galaxies.

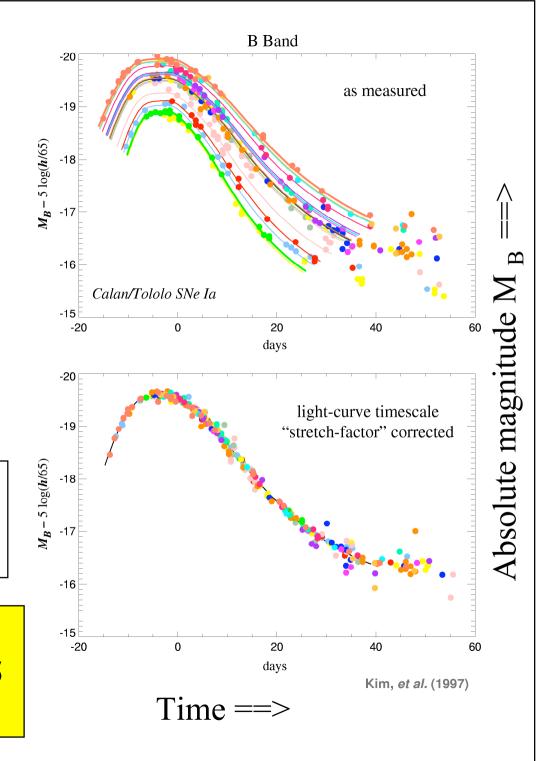
Calibrating "Standard Bombs"

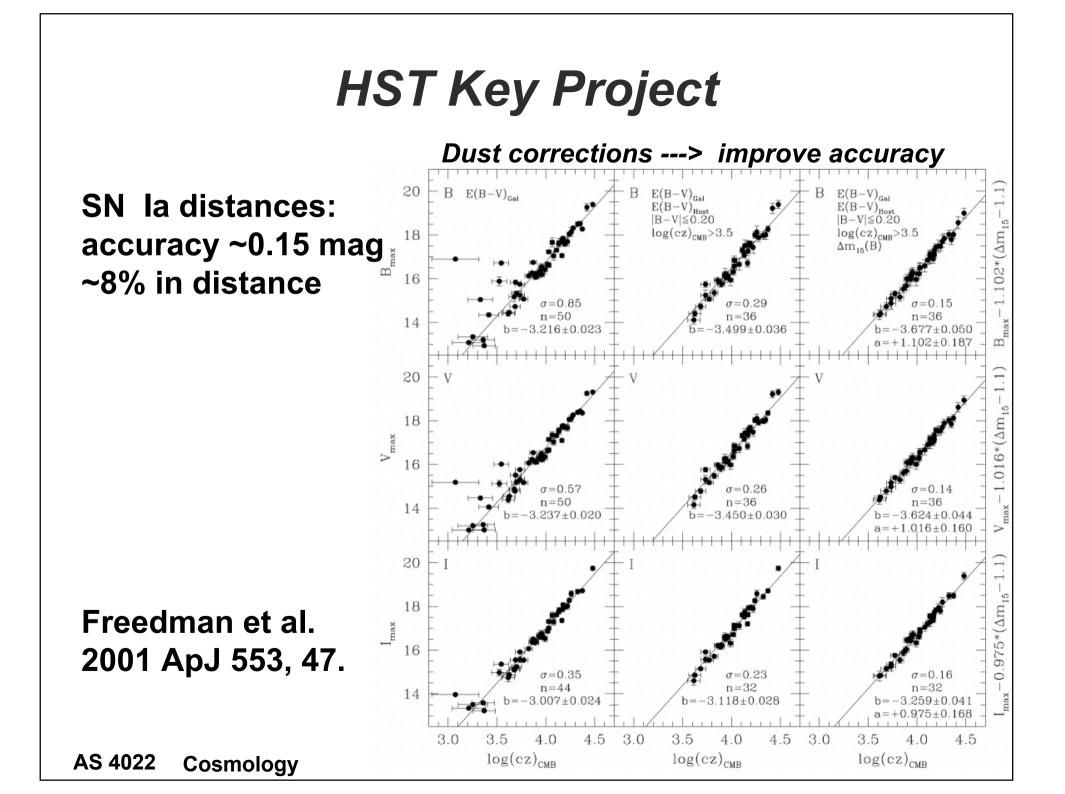
1. Brighter ones decline more slowly.

2. Time runs slower by factor (1+z).

AFTER correcting: Constant peak brightness $M_B = -19.7$

Observed peak magnitude: m = M + 5 log (d/Mpc) + 25 gives the distance!





Galaxy Luminosity Calibrations

$$L = 4\pi D^2 F = K V^4$$

$$D = V^2 \sqrt{\frac{K}{4\pi F}}$$

Determine K using galaxies with Type la Supernovae.

Measure flux F and velocity V to determine distance D.

Tully - Fisher relation

spirals : V = rotation velocity

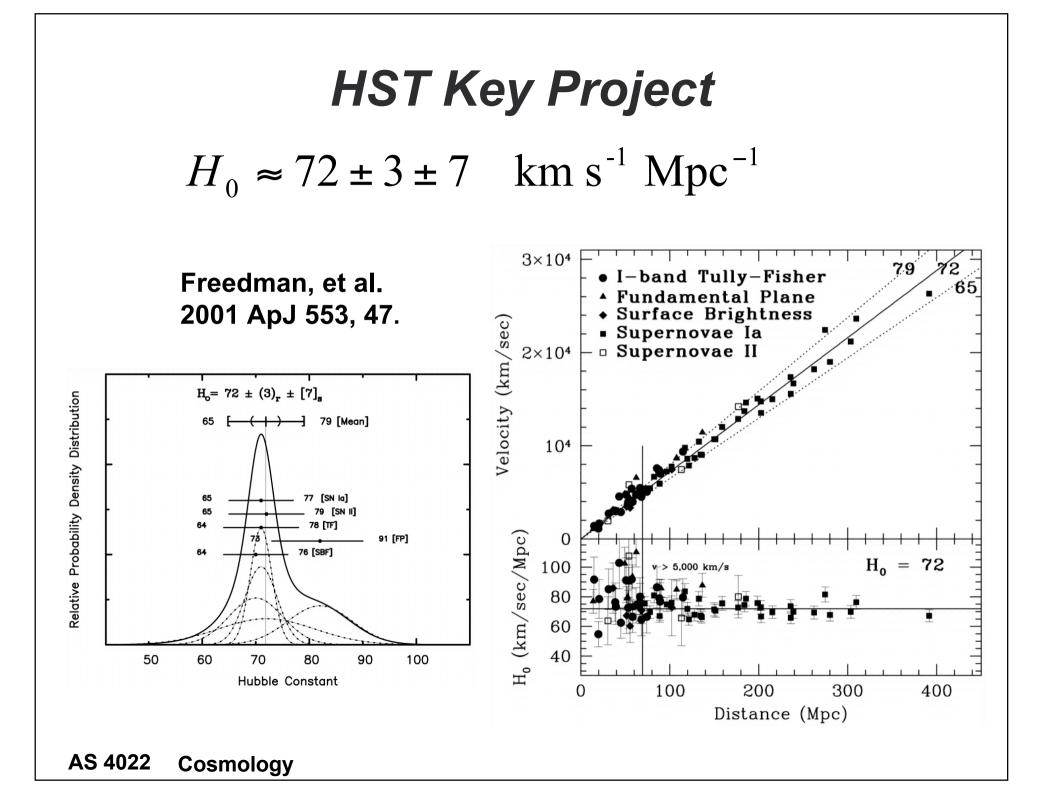
(HI 21 cm emission line width)

Faber - Jackson relation

ellipticals : V = stellar velocity dispersion

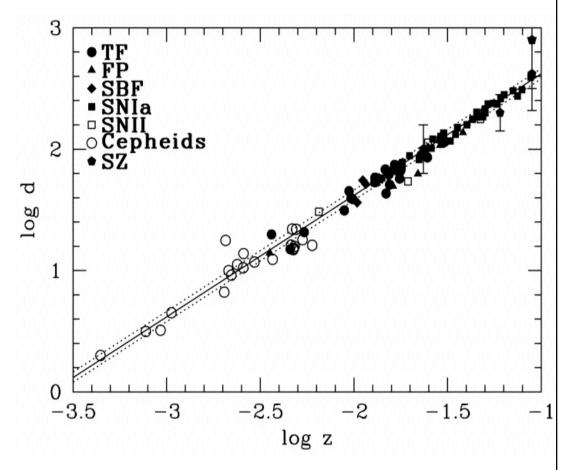
(optical absorption line widths)

"The Fundamental Plane of Ellipticals" improves the F-J relation by including a surface brightness correction.



Frailty of the Distance Ladder

- Parallax
 - 0 300 pc
 - (GAIA 2015 5 kpc)
- Cepheids
 - ~100 pc 20 Mpc (HST)
- Type Ia SNe
 - 20 400 Mpc (8m)
 - z ~ 1.5 (HST)
- Little overlap between Cepheids and SN Ia.



Only 3 galaxies with both Cepheids and SN Ia