Lecture 10

Checking the Distance Ladder:

Sunyaev-Zeldovich Effect

Gravitational Lensing

"Concordance" Model



- 2. Galaxy Counts + M/L ratios $\Omega_{\rm M} \sim 0.3$
- 3. Flat Geometry (inflation, CMB fluctuations) $\Omega_0 = \Omega_M + \Omega_\Lambda = 1$







2





Frailty of the Distance Ladder

- Parallax
 - 0 300 pc
 - (GAIA 2015 5 kpc)
- Cepheids
 - ~100 pc 20 Mpc (HST)
- Type Ia SNe
 - 20 400 Mpc (8m)
 - z ~ 1.5 (HST)
- Little overlap between Cepheids and SN Ia.



Only 3 galaxies with both Cepheids and SN Ia



Galaxy Clusters are filled with hot X-ray gas





Coma cluster

X-ray (hot gas)

Sunyaev - Zeldovich (SZ) effect

Silhouettes of the Hot Cluster Gas seen against the CMB.

CMB photons scattered by hot electrons

 $T \to T \ e^{-\tau} \qquad \Delta T \approx T \ \tau$

scattering optical depth:

 $\tau = n_e \ \sigma \ l$

X - ray emission by hot gas:

$$F_{X} = \frac{L_{X}}{4\pi D_{L}^{2}} \qquad L_{x} \approx a(T_{x}) n_{e}^{2} l^{3}$$

angular diameter :

$$\theta = \frac{l}{D_A}$$

Note: assume smooth density and spherical symmetry of hot gas Scattered CMB photons shift to higher energy (Inverse Compton).

CMB photons

X-ray gas (hot

electrons T~107K)

T~3K)

SZ Distances

Eliminate unknown *n*_e

$$\frac{L_X}{\tau^2} = \frac{a n_e^2 l^3}{\left(n_e \sigma l\right)^2} = \frac{a}{\sigma^2} l = \frac{a}{\sigma^2} \theta D_A$$
$$= \frac{4\pi D_L^2 F_X}{\left(\Delta T/T\right)^2}$$

Solve for distance:

$$\frac{D_{L}^{2}}{D_{A}} = \frac{\left[r_{0}\left(1+z\right)\right]^{2}}{r_{0}/\left(1+z\right)} = r_{0}\left(1+z\right)^{3} = \frac{a(T_{X})}{4\pi\sigma^{2}}\left(\frac{\Delta T}{T}\right)^{2}\frac{\theta}{F_{X}}$$

Mixture of D_L and D_A

Another observable distance !



Gravitational Lensing

 Luminous arcs in clusters of galaxies



Gravitational Lensing

multiple images

of background galaxy lensed by the cluster



The Lensed Galaxy



AS 4022











Lensing by a Point Mass

2 images opposite sides of lens major image outside ring minor image inside ring



Point Moss Lens

net magnification (sum of 2 images) vs time uoitooti N -1 $x/R_E = (t-t_0)/t_E$



angular diameter distances from redshifts: z_L , z_S impact parameter: $b = D_L \theta$ source offset : $D_S \theta_S = D_S \theta - D_{LS} \alpha$ bend angle: $\alpha = (\theta - \theta_S) \frac{D_S}{D_{LS}} = \frac{4 G M(<b)}{c^2 b}$



Quasars Lensed by Galaxies



Masses from Einstein Rings

Perfect alignment gives an Einstein Ring

$$\theta_E = \frac{R_E}{D_L} = \left(\frac{4 \ G \ M}{c^2} \frac{D_{LS}}{D_L D_S}\right)^{1/2}$$
$$\frac{\theta_E}{\operatorname{arcsec}} = \left(\frac{M}{10^{11} M_{sun}}\right)^{1/2} \left(\frac{D_L D_S / D_{LS}}{Gpc}\right)^{-1/2}$$
$$\frac{M}{10^{11} M_{sun}} = \frac{D_L D_S / D_{LS}}{Gpc} \left(\frac{\theta_E}{\operatorname{arcsec}}\right)^2$$



Use redshifts, z_L, z_S , for the angular diameter distances.

Or, if mass known, e.g
$$M \approx \frac{V^2 R}{G}$$
, then θ gives D
Mass usually less certain than distance,

so use theta and D to calculate M.



light travel time delay:

$$c \Delta t = \left(D_L^2 + b^2\right)^{1/2} + \left(D_{LS}^2 + b^2\right)^{1/2} - \left(D_L + D_{LS}\right)$$
$$= D_L \left[\left(1 + \theta^2\right)^{1/2} - 1\right] + D_{LS} \left[\left(1 + \left(\frac{D_L}{D_{LS}}\theta\right)^2\right)^{1/2} - 1\right]$$
$$= D_L \frac{\theta^2}{2} \left(1 + \frac{D_L}{D_{LS}}\right) \approx \frac{c z_L}{H_0} \frac{\theta^2}{2} \left(1 + \frac{z_L}{z_S - z_L}\right) = \frac{c}{H_0} \frac{\theta^2}{2} \left(\frac{z_L z_S}{z_S - z_L}\right)$$
measure θ (images), z_L, z_S (spectra)
and Δt (delay from lightcurves of images)

and Δl (delay from lightcurves of images).

Time Delay Measurement

Light curves of the images show a shift in time.



But, no simple lenses.

Almost always several galaxies involved.

Prevents very accurate distance measurements.

