

AS1001:Extra-Galactic Astronomy

Lecture 3: Galaxy Fundamentals

Galaxy Fundamentals

- How many stars are in a galaxy ?
- How did galaxies form ?
- How many galaxies are there ?
- How far apart are they ?
- How are they clustered ?
- What is the mass of a typical galaxy ?
- What is the mass density of the Universe ?

Extra-galactic Distances

For extragalactic distances, convenient unit is $1 \text{ Mpc} = 10^6 \text{ pc}$

$$\begin{aligned} m - M &= 5 \log_{10}(d / \text{pc}) - 5 \\ &= 5 \log_{10}\left(\frac{d}{\text{pc}} \times \frac{10^6 \text{ pc}}{\text{Mpc}}\right) - 5 \\ &= 5 \log_{10}(d / \text{Mpc}) + 5 \log_{10}(10^6) - 5 \\ &= 5 \log_{10}(d / \text{Mpc}) + 25 \end{aligned}$$

Note: Still have $m = M$ at $d = 10 \text{ pc}$

How many stars in a Galaxy ?

M31 (Andromeda), at 0.9 Mpc, has an apparent magnitude $m_v = +3.5$ mag

1) $M = m - 5 \log_{10}(d/\text{Mpc}) - 25 = -21.3$ mag

2) Assume $M_* = +5.5$ (Sun-like stars)

3) $F_{GAL} = n_* F_*$

$$M_{GAL} - M_* = -2.5 \log_{10} \left(\frac{F_{GAL}}{F_*} \right) = -2.5 \log_{10} (n_*)$$

4) $n_* = \frac{F_{GAL}}{F_*} = 10^{-(M_{GAL} - M_*)/2.5} = 10^{-(-21.3 - 5.5)/2.5} \approx 5 \times 10^{10}$

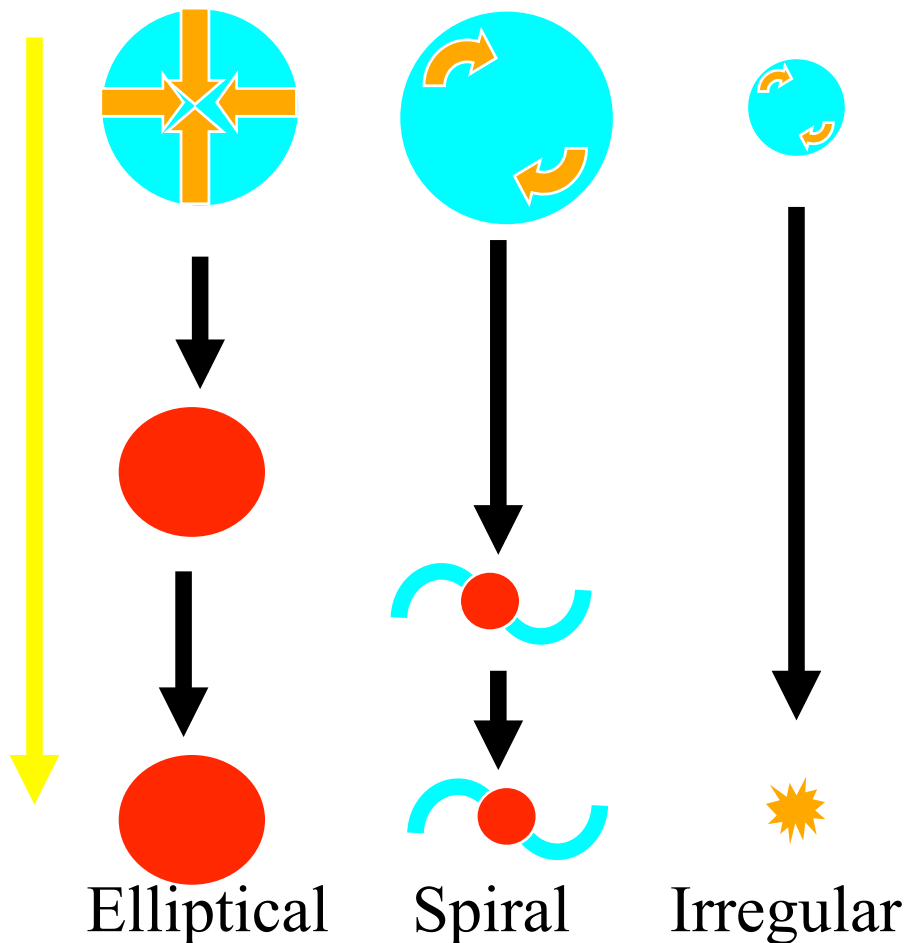
$n_* = 50$ billion stars

How did Galaxies Form ?

TWO COMPETING SCENARIOS

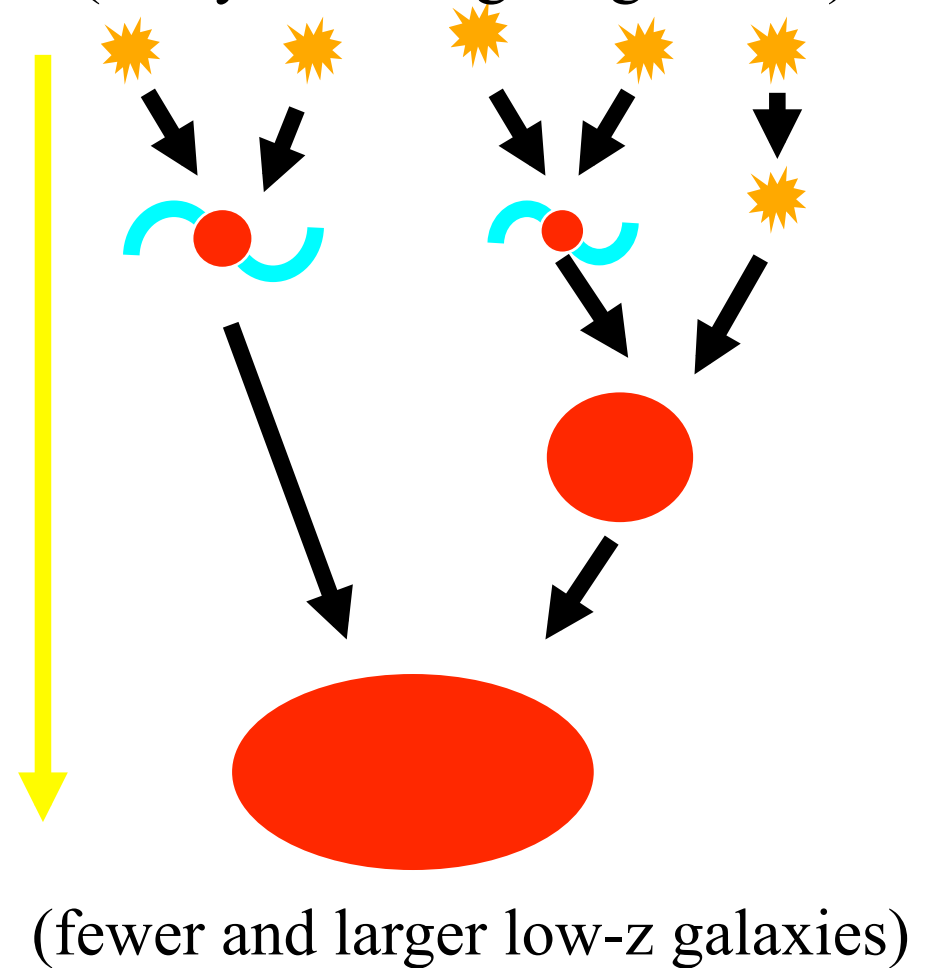
Initial Collapse:

(rotation => slower collapse)



Hierarchical Merging:

(many small high-z galaxies)



How did Galaxies Form?

Initial Collapse

- **For:**
 - Nearby Ellipticals are old
 - Ellipticals seen at high z
 - Spirals/Irrs rotating
 - Irregulars forming today
- **Against:**
 - Mergers are seen

Hierarchical Merging

- **For:**
 - Mergers are seen
 - More Ellipticals in high density clusters
 - HST sees more small Irrs at high z
- **Against:**
 - Some large Ellipticals seen at high z
 - Irregulars forming today

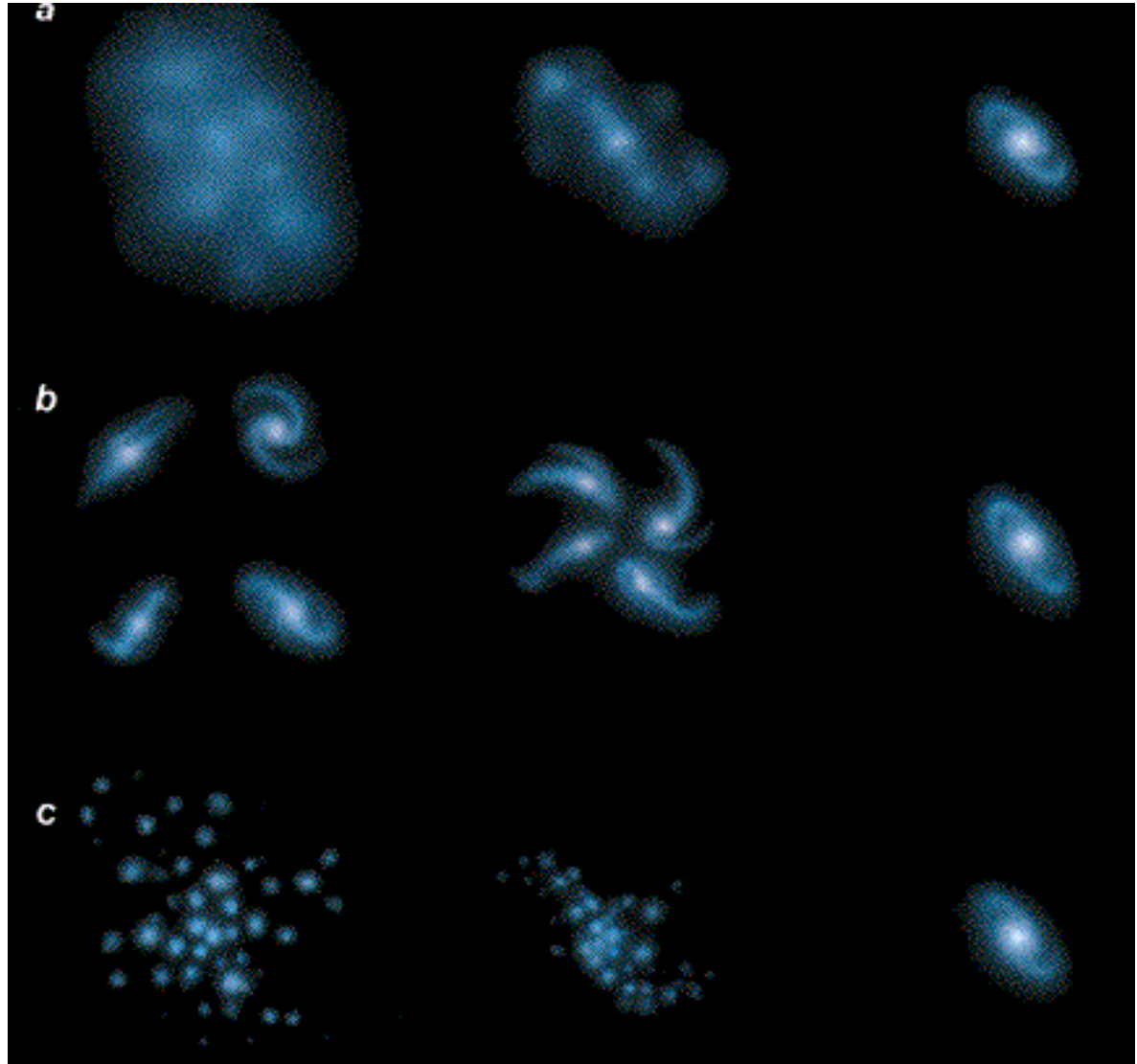
PROBABLY BOTH OCCUR

Galaxy Formation Scenarios

Initial Collapse:

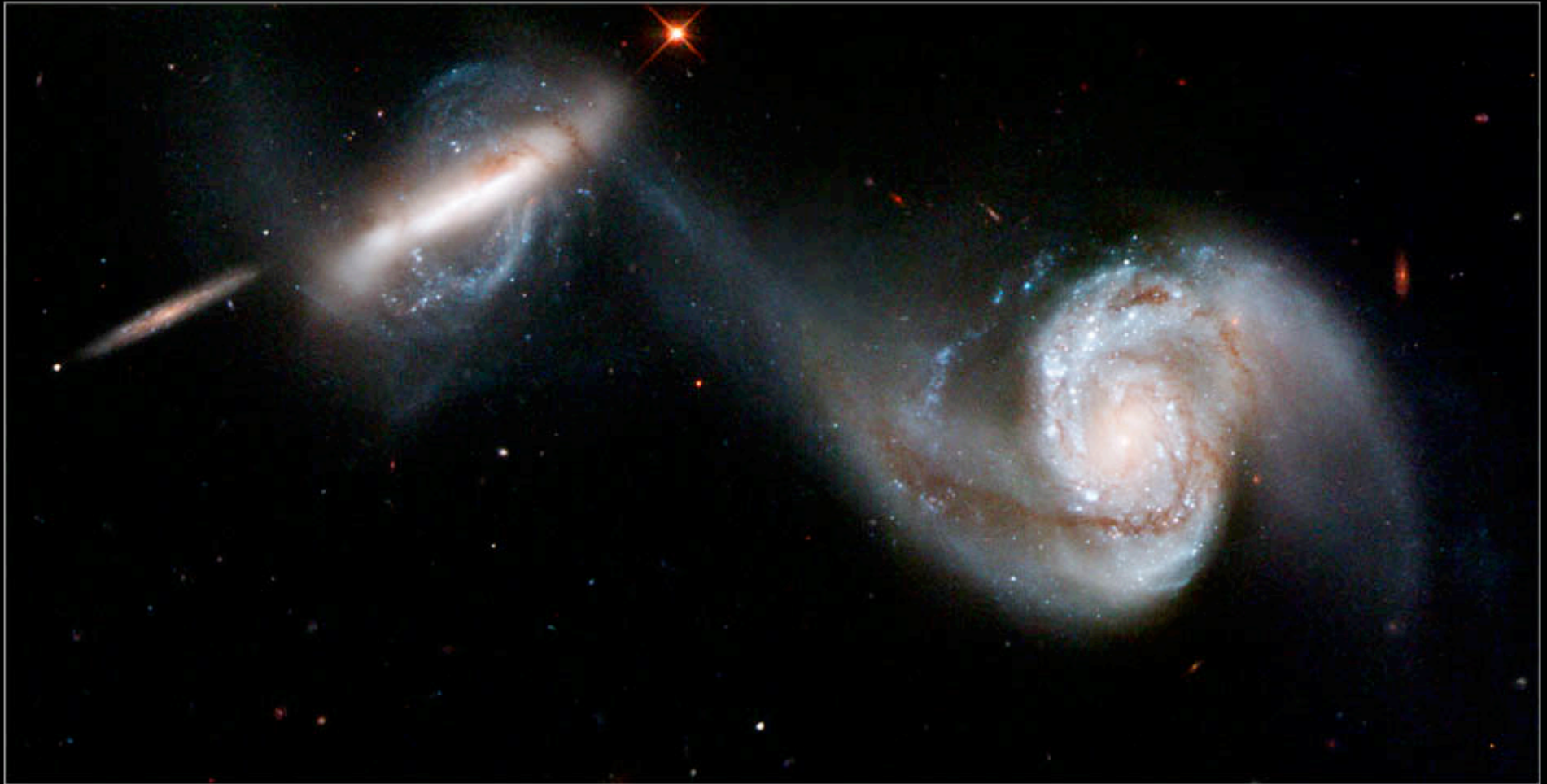
Followed by merging:

Hierarchical merging:



Colliding Galaxies

Interacting Galaxies • Arp 87



Hubble
Heritage

Colliding Galaxies

NGC 6050

Arp 148



The Antennae Galaxy: mid-merger



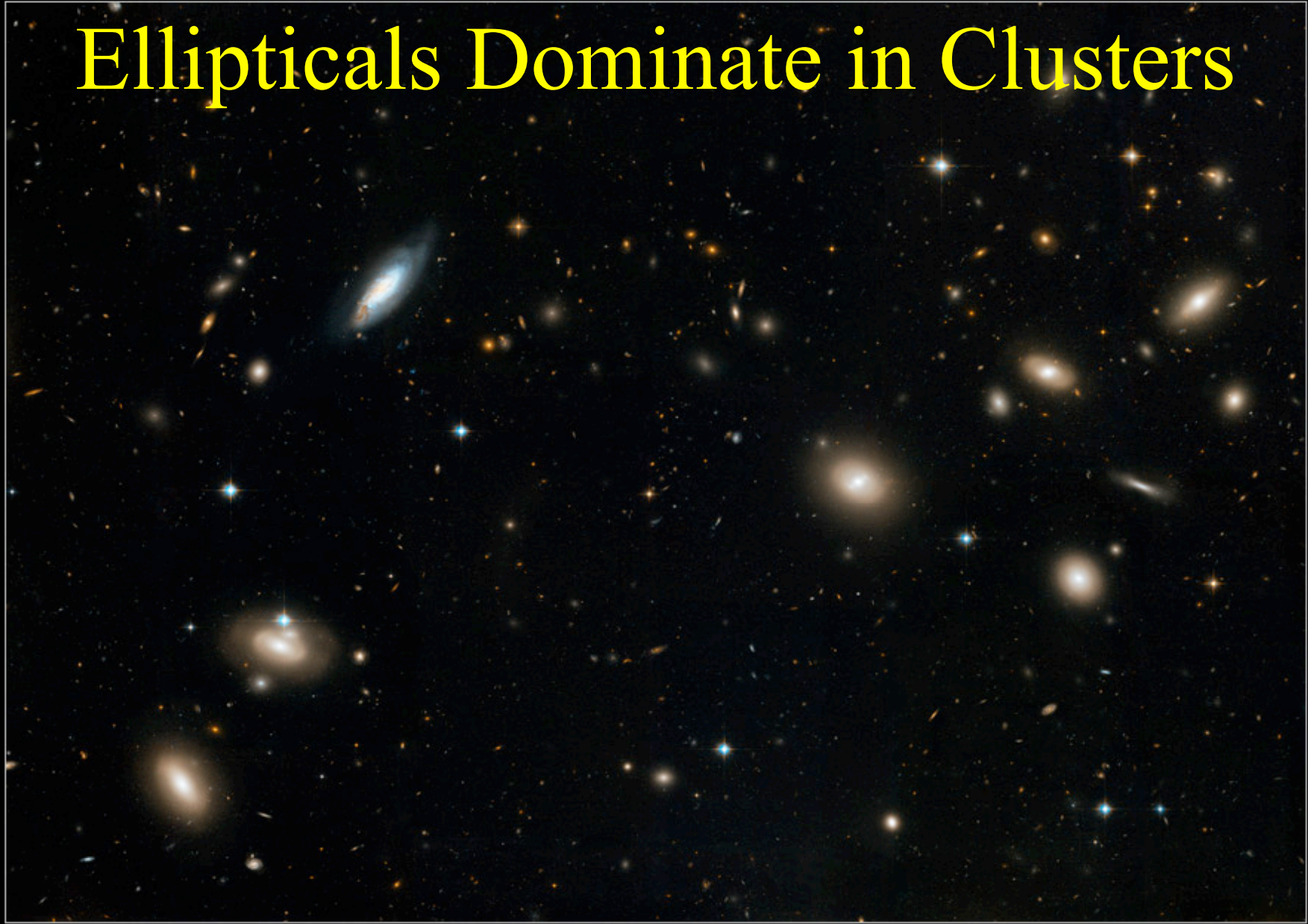
Colliding Galaxies NGC 4038 and NGC 4039

HST • WFPC2

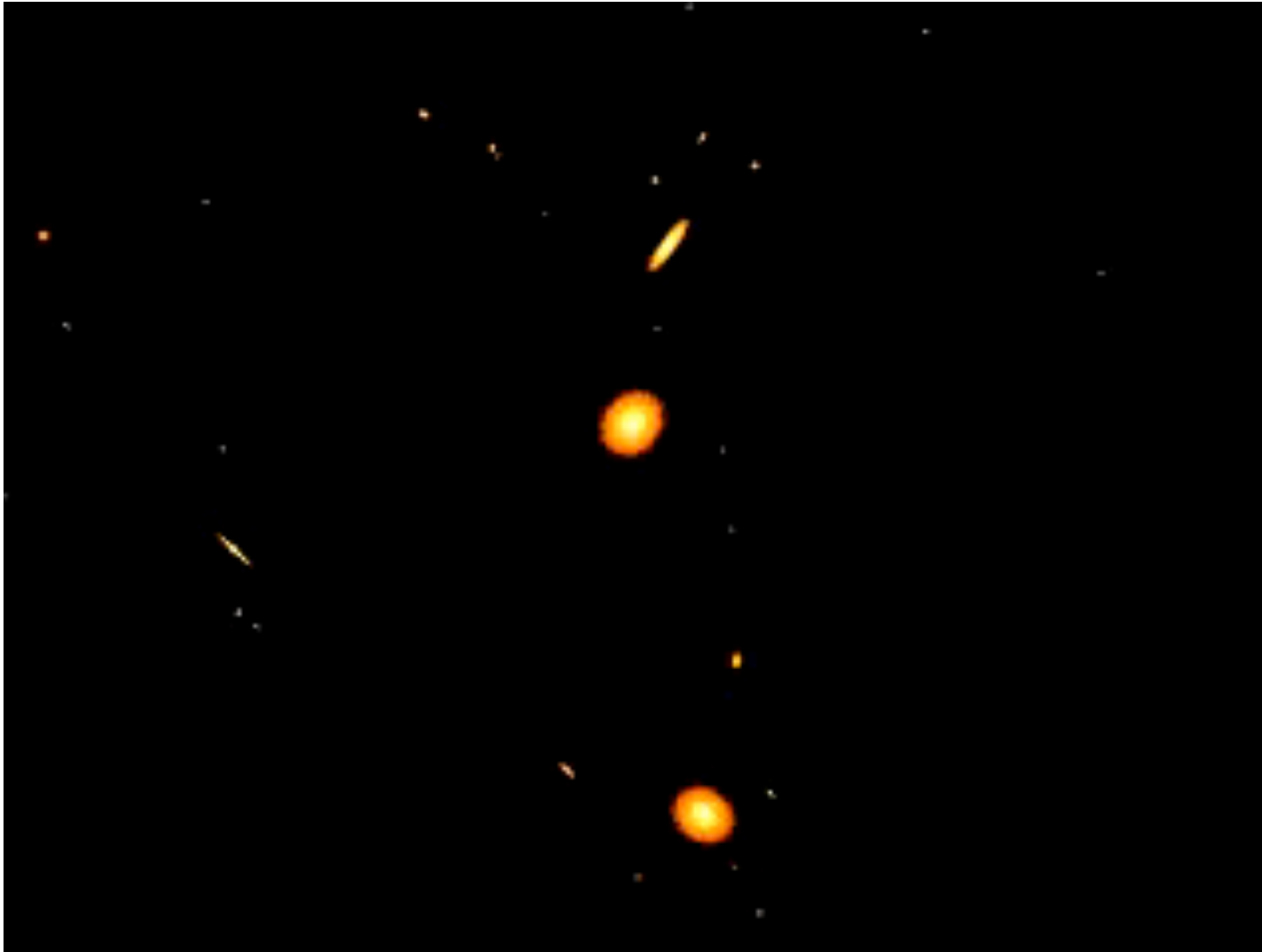
PRC97-34a • ST ScI OPO • October 21, 1997 • B, Whitmore (ST ScI) and NASA

Coma Cluster of Galaxies

Ellipticals Dominate in Clusters

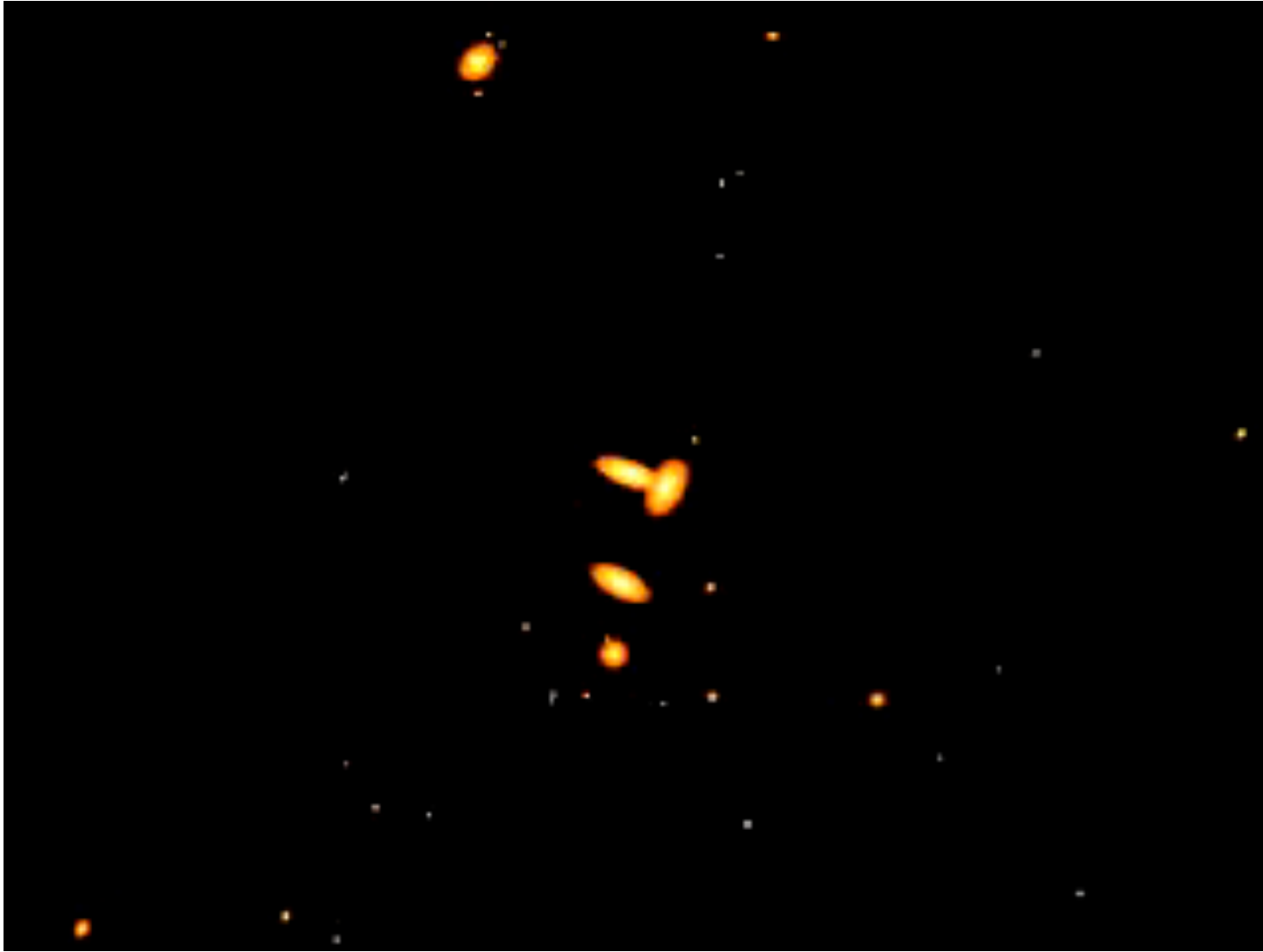


Cluster Formation Simulation



“Galactic Canibalism”: forms a giant galaxy at the cluster centre.

Cluster Formation Simulation



“Galactic Cannibalism”: forms a giant galaxy at the cluster centre.

How many galaxies are there ?

STEP1: Take all-sky photos

STEP2: Count galaxies brighter than some magnitude

STEP3: Assume most galaxies are like the MW*

STEP4: Calculate depth and volume of sky

STEP5: Calculate the SPACE DENSITY of galaxies

[* Big bright galaxies like the Milky Way are easiest to detect.

This does not mean they are the most numerous, just the most visible !]

Space Density of Galaxies

- **Example: The MW has $M_B = -20$ mag. There are $\sim 10^4$ MW-like galaxies brighter than 14th mag over the whole sky. How many galaxies are there per $(\text{Mpc})^3$?**

Distance modulus equation gives the depth of the survey, i.e. the maximum distance \Rightarrow

Volume of the survey \Rightarrow

$n =$ number density

$$m - M = 5 \log_{10}(d / \text{Mpc}) + 25$$

$$d = 10^{(m-M-25)/5} = 10^{(14-(-20)-25)/5} \\ = 63 \text{ Mpc}$$

$$\text{Vol} = \frac{4\pi}{3} d^3 = \frac{4\pi}{3} (63 \text{ Mpc})^3 \\ = 10^6 \text{ Mpc}^3$$

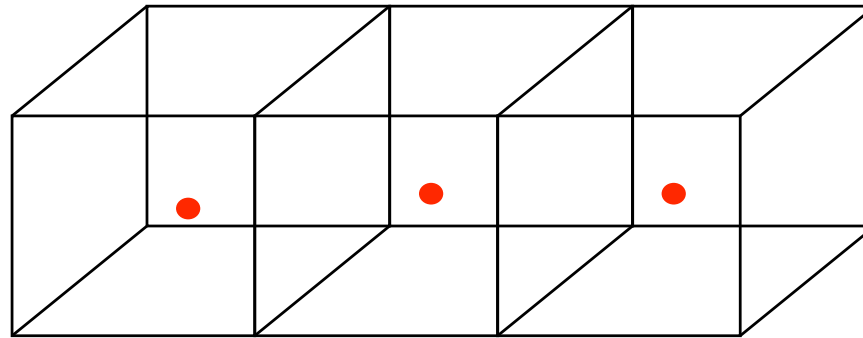
$$n = \frac{N}{\text{Vol}} = \frac{10^4 \text{ gals}}{10^6 \text{ Mpc}^3} = 10^{-2} \frac{\text{gals}}{\text{Mpc}^3}$$

There is ~ 1 MW-like galaxy per 100 Mpc^3

How far apart are they ?

Typical separation between galaxies:

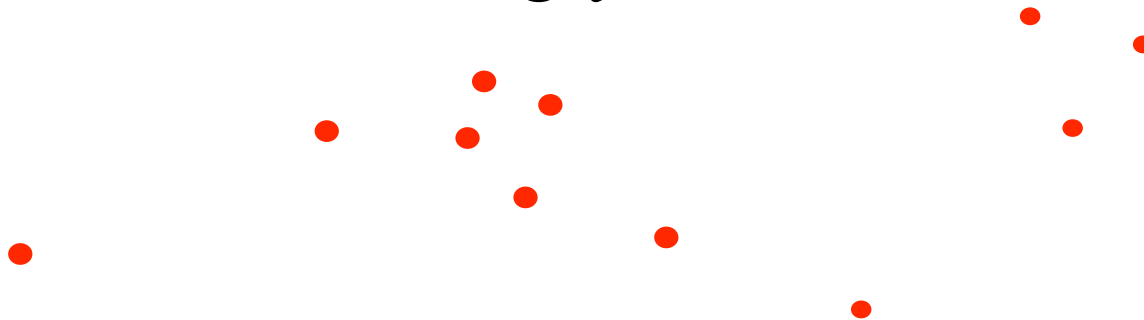
$$\sim (100 \text{ Mpc}^3)^{1/3}$$
$$= 4.6 \text{ Mpc}$$



4.6 Mpc

Volume:
100 Mpc³

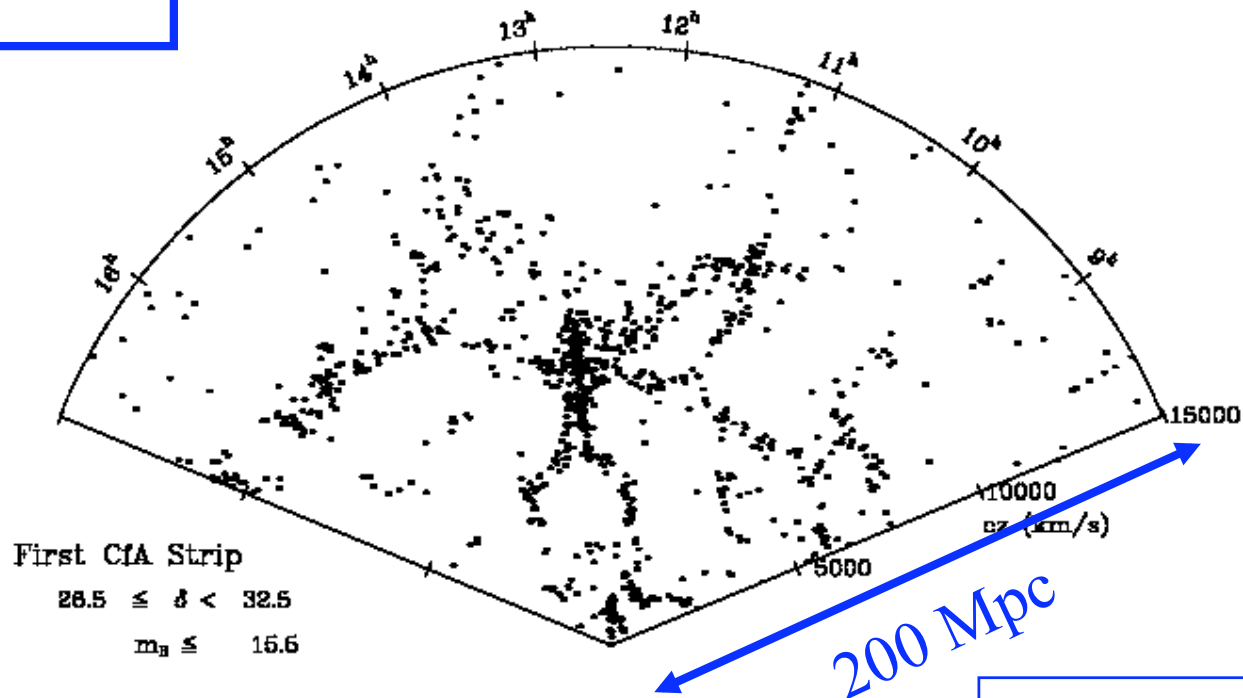
However, galaxies are strongly clustered.



Large Scale Structure

Galaxy Redshift Surveys

“The Stickman”: 1980



$$d = v / H_0 = c z / H_0$$

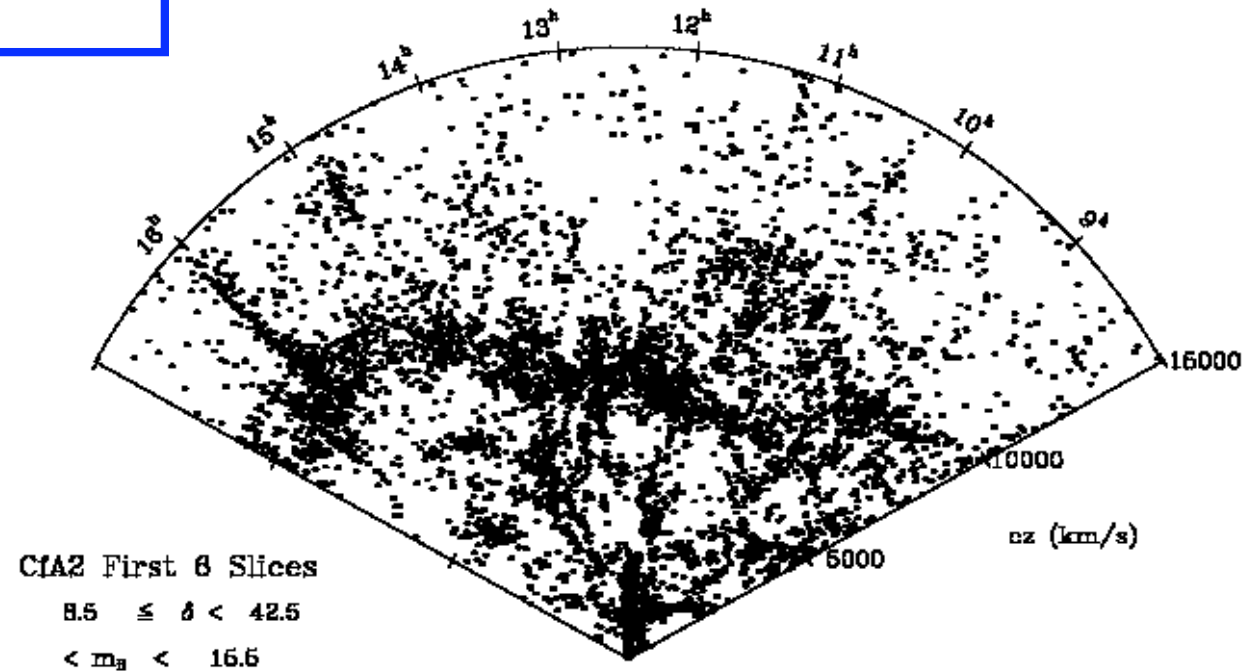
Geller & Huchra

Hubble's Law used to determine distances

Large Scale Structure

Galaxy Redshift
Surveys

“The Great Wall”: 1988

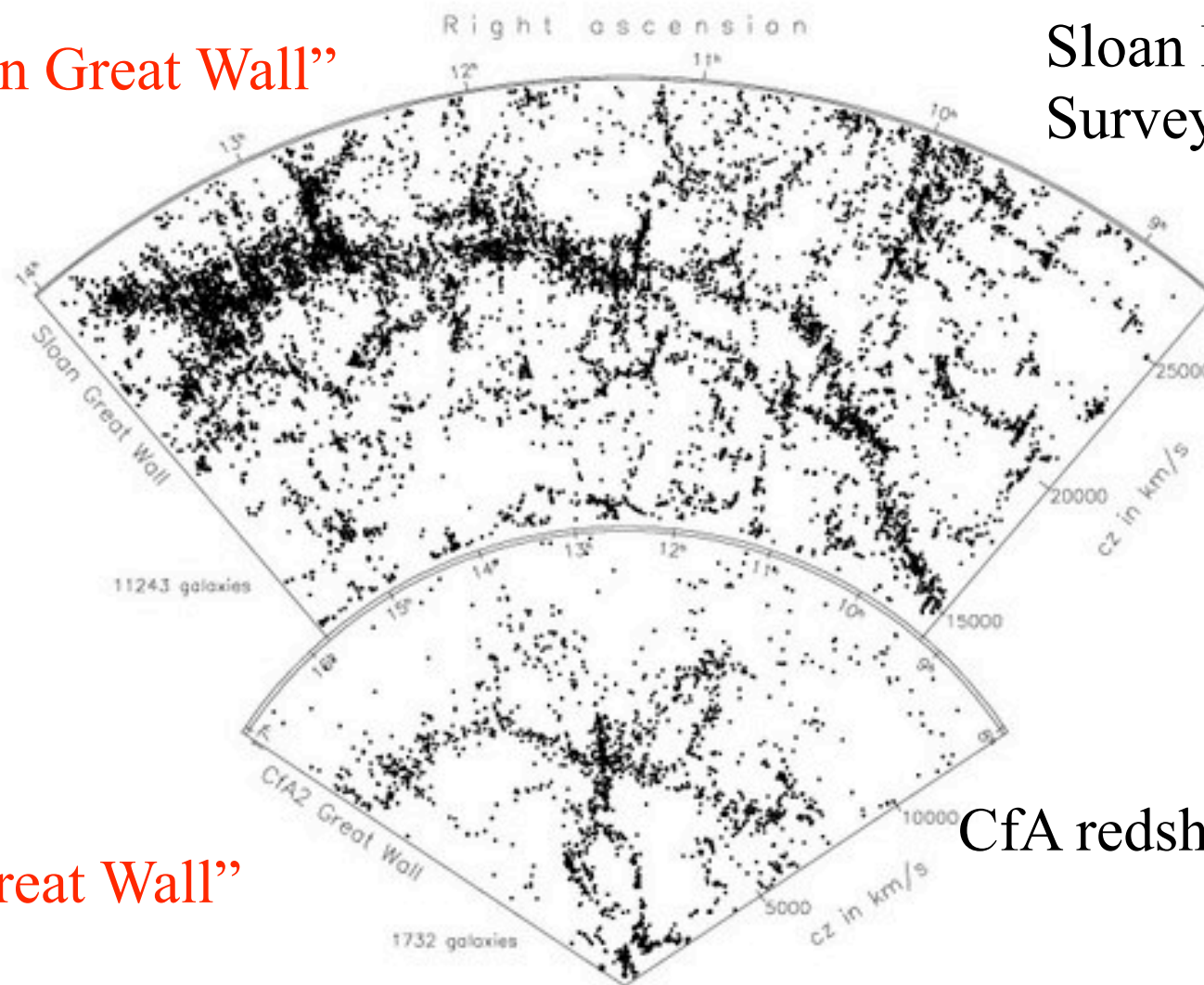


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Large Scale Structure

“Sloan Great Wall”

Sloan Digital Sky Survey (SDSS)



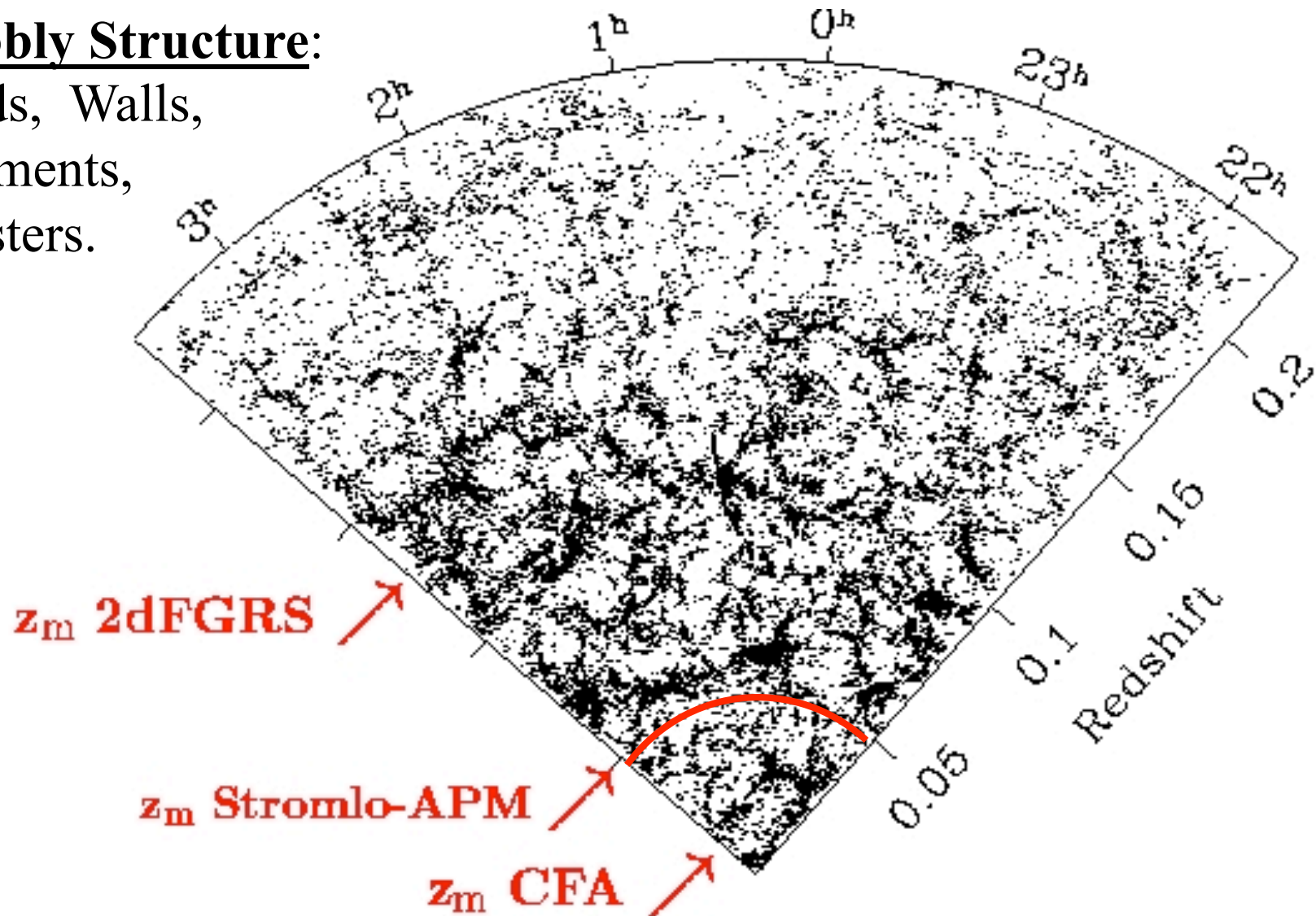
“Great Wall”

CfA redshift survey

Large Scale Structure

Bubbly Structure:

Voids, Walls,
Filaments,
Clusters.



Mass-to-Light Ratios

- Assume that a galaxy's luminosity is proportional to its mass
- i.e., there is a **mass-to-light** ratio
- Expressed in solar units:

Mass-to-light ratio \longrightarrow $\frac{M}{L} = X \frac{M_{\odot}}{L_{\odot}}$

\longleftarrow Solar Mass

\longleftarrow Solar Luminosity

$X = 1$ for our Sun

$X \sim 10$ for a typical Galaxy

The Mass of Andromeda (M31)

M31 has $M_V = -21.3$ mag. Determine its mass assuming a “typical” mass-to-light ratio, $X = 10$.

$$\mathbf{M} = \frac{\mathbf{M}}{L} L = 10 \frac{\mathbf{M}_{\odot}}{L_{\odot}} L = 10 \mathbf{M}_{\odot} \frac{L}{L_{\odot}}$$

$$\mathbf{M} = 10 \mathbf{M}_{\odot} 10^{-(M_V(\text{M31}) - M_V(\text{Sun}))/2.5}$$

$$\mathbf{M} = 10 \times (2 \times 10^{30} \text{ kg}) \times 10^{-(-21.3 - 5.4)/2.5}$$

$$\mathbf{M} = 2 \times 10^{41} \text{ kg} = 10^{11} \mathbf{M}_{\odot}$$

Mass Density of the Universe

- Multiply (the **space density** of galaxies)
x (the **mass** of a typical galaxy)
= the mass density of the Universe:

$$\rho = n M \sim \frac{10^{11} M_{\odot}}{100 \text{ Mpc}^3} = 10^9 \frac{M_{\odot}}{\text{Mpc}^3} \approx 10^{-28} \text{ kg / m}^3$$

- This is the **luminous matter**, i.e. the stars (+gas+dust), that we can see.
- However ... **“Dark Matter”** dominates.

Mass Density of the Universe

- More accurate observations (using masses from the velocities of stars inside galaxies, and of galaxies inside clusters) gives a **total density** (including **both luminous and Dark Matter**):

$$\rho \sim 3 \times 10^{10} \frac{M_{\odot}}{\text{Mpc}^3} \sim 3 \times 10^{-27} \text{ kg/m}^3$$

- Most of matter is “Dark Matter” !
- Mass of hydrogen atom: $m_{\text{H}} = 1.7 \times 10^{-27} \text{ kg}$
- Spread the matter smoothly, and there would be only a few hydrogen atoms per m^3 .
- The air we breathe has $\sim 10^{25}$ atoms per m^3 .