AS1001:Extra-Galactic Astronomy

Lecture 3: Galaxy Fundamentals

Galaxy Fundamentals

- How many stars are in a galaxy?
- · How did galaxies form?
- How many galaxies are there?
- How far apart are they?
- How are they clustered?
- What is the mass of a typical galaxy?
- What is the mass density of the Universe?

Extra-galactic Distances

For extragalactic distances, convenient

unit is
$$1 \text{ Mpc} = 10^6 \text{ pc}$$

 $m - M = 5 \log_{10}(d/\text{pc}) - 5$

$$= 5 \log_{10} \left(\frac{d}{\text{pc}} \times \frac{10^6 \text{ pc}}{\text{Mpc}} \right) - 5$$

=
$$5 \log_{10}(d/\text{Mpc}) + 5 \log_{10}(10^6) - 5$$

= $5 \log_{10}(d/\text{Mpc}) + 25$

Note: Still have m = M at d = 10 pc

How many stars in a Galaxy?

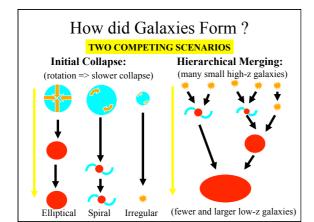
M31 (Andromeda), at 0.9 Mpc, has an apparent magnitude $m_v = +3.5$ mag

- 1) $M = m 5 \log_{10}(d/\text{Mpc}) 25 = -21.3 \text{ mag}$
- 2) Assume $M_* = +5.5$ (Sun-like stars)
- $3) \quad F_{GAL} = n_* \, F_*$

$$M_{GAL} - M_* = -2.5 \log_{10} \left(\frac{F_{GAL}}{F_*} \right) = -2.5 \log_{10} (n_*)$$

4)
$$n_* = \frac{F_{GAL}}{F_*} = 10^{-(M_{GAL}-M_*)/2.5} = 10^{-(-21.3-5.5)/2.5} \approx 5 \times 10^{10}$$

 $n_* = 50$ billion stars



How did Galaxies Form?

Initial Collapse

For:

- Nearby Ellipticals are old
- Ellipticals seen at high z
- Spirals/Irrs rotating
- Irregulars forming today

Against:

- Mergers are seen

Hierarchical Merging

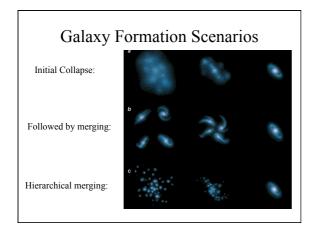
· For:

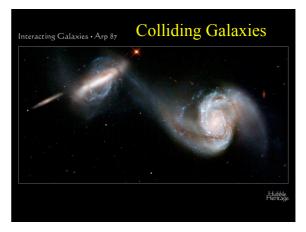
- Mergers are seen
- More Ellipticals in high density clusters
- HST sees more small Irrs at high z

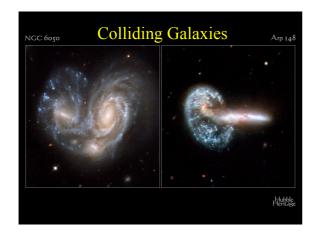
· Against:

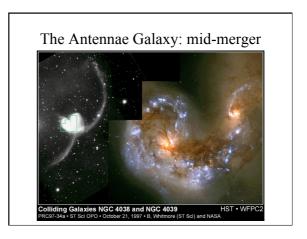
- Some large Ellipticals seen at high z
- Irregulars forming today

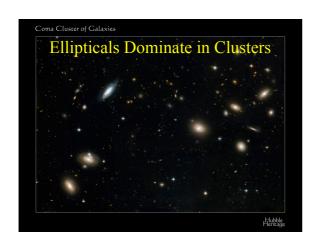
PROBABLY BOTH OCCUR

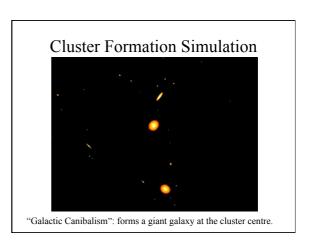












Cluster Formation Simulation

"Galactic Canibalism": forms a giant galaxy at the cluster centre.

How many galaxies are there?

STEP1: Take all-sky photos

STEP2: Count galaxies brighter than some magnitude

STEP3: Assume most galaxies are like the MW*

STEP4: Calculate depth and volume of sky

STEP5: Calculate the SPACE DENSITY of galaxies

[* Big bright galaxies like the Milky Way are easiest to detect.

This does not mean they are the most numerous, just the most visible!]

Space Density of Galaxies

Example: The MW has $M_B = -20$ mag. There are $\sim 10^4$ MW-like galaxies brighter than 14th mag over the whole sky. How many galaxies are there per (Mpc)³ ?

Distance modulus equation gives the depth of the survey, i.e. the maximum distance =>

Volume of the survey =>

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n = number density

 $m - M = 5\log_{10}(d / \text{Mpc}) + 25$ $d = 10^{(m-M-25)/5} = 10^{(14-(-20)-25)/5}$ = 63 Mpc

 $Vol = \frac{4\pi}{3} d^3 = \frac{4\pi}{3} (63 \text{Mpc})^3$ $= 10^6 \text{ Mpc}^3$

 $a = \frac{N}{\text{Vol}} = \frac{10^4 \text{gals}}{10^6 \text{ Mpc}^3} = 10^{-2} \frac{\text{gals}}{\text{Mpc}^3}$

There is ~1 MW-like galaxy per 100 Mpc³

How far apart are they?

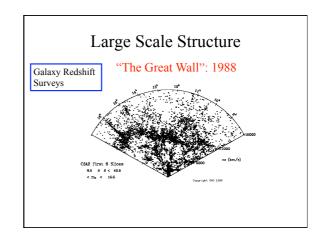
Typical separation between galaxies:

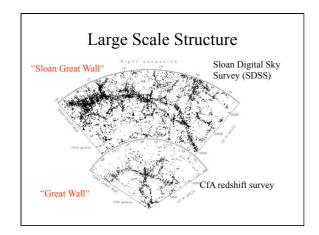
 $\sim (100 \text{ Mpc}^3)^{1/3}$ = 4.6 Mpc

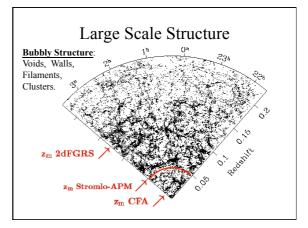
Volume:
4.6 Mpc

100 Mpc³

However, galaxies are strongly clustered.

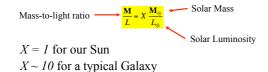






Mass-to-Light Ratios

- Assume that a galaxy's luminosity is proportional to its mass
- i.e., there is a mass-to-light ratio
- Expressed in solar units:



The Mass of Andromeda (M31)

M31 has $M_V = -21.3$ mag. Determine its mass assuming a "typical" mass-to-light ratio, X = 10.

$$\mathbf{M} = \frac{\mathbf{M}}{L} L = 10 \frac{\mathbf{M}_{\odot}}{L_{\odot}} L = 10 \ \mathbf{M}_{\odot} \frac{L}{L_{\odot}}$$

$$\mathbf{M} = 10 \ \mathbf{M}_{\odot} 10^{-(M_{\rm V}({\rm M31}) - M_{\rm V}({\rm Sun}))/2.5}$$

$$\mathbf{M} = 10 \times (2 \times 10^{30} \,\mathrm{kg}) \times 10^{-(-21.3 - 5.4)/2.5}$$

$$\mathbf{M} = 2 \times 10^{41} \text{kg} = 10^{11} M_{\odot}$$

Mass Density of the Universe

- Multiply (the **space density** of galaxies)
 - x (the mass of a typical galaxy)
 - = the mass density of the Universe:

$$\rho = n \,\mathbf{M} \sim \frac{10^{11} \,\mathbf{M}_{\odot}}{100 \,\mathrm{Mpc}^3} = 10^9 \,\frac{\mathbf{M}_{\odot}}{\mathrm{Mpc}^3} \approx 10^{-28} \,\mathrm{kg} \,/\,\mathrm{m}^3$$

- This is the **luminous matter**, i.e. the stars (+gas+dust), that we can see.
- However ... "Dark Matter" dominates.

Mass Density of the Universe

 More accurate observations (using masses from the velocities of stars inside galaxies, and of galaxies inside clusters) gives a total density (including both luminous and Dark Matter):

$$\rho \sim 3 \times 10^{10} \frac{M_{\odot}}{\text{Mpc}^3} \sim 3 \times 10^{-27} \text{kg/m}^3$$

- Most of matter is "Dark Matter"!
- Mass of hydrogen atom: $m_H = 1.7x10^{-27} \text{ kg}$
- Spread the matter smoothly, and there would be only a few hydrogen atoms per m³.
- The air we breathe has $\sim 10^{25}$ atoms per m³.